

Comparative Performance of Steel Drainage Pipes against Flood-induced Deformation in River Levee

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Abstract

Steel drainage pipes that can provide both drainage and reinforcement functions are expected to give better performance in levee protection against flooding compared to the protection that can provide only either one of these functions. This study investigates the effectiveness of steel drainage pipes that combine the drainage and reinforcement functions against flooding in comparison with the pipes having only either drainage or reinforcement function through the finite element analysis validated by the simulation of the centrifuge model tests. The analysis results reveal that drainage function is crucial in minimisation of deformation, while the use of steel drainage pipe protection is more reliable as protection is available in form of reinforcement even when drainage function has deteriorated. Levee protected only with reinforcement and only drainage pipes experienced 112% and 2.4% larger settlements respectively in comparison to levees protected with steel drainage pipes. The performance of a levee reinforced by steel drainage pipe against flooding is more redundant and reliable compared to the traditional method of protection which provides only one of the functions.

Keywords: levee; seepage; finite element analysis; steel drainage pipes

1 Introduction

2 River levees during the flooding event in the absence of the proper protection sometimes
3 experience a large deformation, and in the worst-case scenario, even the breaching of the levee
4 is observed. Deformation is the result of the reduction of matric suction due to saturation of
5 the levee caused due to increased seepage flow during the flood (Hamdhan and Schweiger,
6 2011; Polemio and Lollino, 2011; Vandamme and Zou, 2013). Traditionally, there are two
7 different approaches to designing the protection measures in the levee. The first method of
8 protection is providing additional strength through reinforcement, (Rotte and Viswanadham,
9 2012; Yang and Deng, 2019; Zhou et al., 2009) and another method is minimising the strength
10 reduction through drainage (Rahardjo et al., 2003, 2011; Saran and Viswanadham, 2018). In
11 this study use of steel drainage pipe which combines both traditional approaches of protection
12 by providing drainage and reinforcement is proposed.

13 Steel drainage pipes are tubular steel pipes with numerous holes on the surface and also have
14 spiral blades at the end. Steel drainage pipes because of their tubular structures, surface holes,
15 and spiral blades can provide both reinforcement and drainage functions. A Series of centrifuge
16 experiments were performed by Singh et al. (2019) to understand the working mechanism of
17 these steel drainage pipes. Unfortunately, as the same flood pattern could not be given to all
18 the models, the relative performance of the steel drainage pipe could not be confirmed. In this
19 paper, through finite element modelling, a comparative study of steel drainage performance
20 against its traditional counterpart with only either drainage or reinforcement function is made
21 under the same flooding condition.

22 A Series of the six different cases of the centrifugal tests were performed at the centrifugal
23 acceleration of 20g by Singh et al. (2019). Centrifuge experiments were performed for its
24 better capillary condition and realistic stress condition in the physical model ground. For all

25 the test cases, a half section of the river levee made of Edosaki sand with a side slope of 1H:
26 1V was modelled. Six different cases of varying levels of protection were investigated during
27 the study. In the centrifuge study since the same level of flooding was not achieved, direct
28 comparison to study performance was rather difficult. For this purpose, a numerical simulation
29 of four different cases of unreinforced levee case, the levee with proposed steel drainage pipes,
30 the case with only reinforcement pipes and the case with drainage pipes is presented in this
31 study. Four of the cases and their test conditions are summarised in **Table 1**. **Figure 1** shows
32 the geometry of the model slope and arrangement of pipes in the centrifuge models. Here and
33 after all the dimensions are in the prototype scale. In Cases 3, 4, and 6, pipes are installed at a
34 1m height from the toe of the slope. The model consisted of three sections; the water supply
35 section, the model ground section, and the drainage section collecting drained seepage water.
36 In Cases 3, 4, and 6, three pipes were installed at a horizontal spacing of 1 m and an elevation
37 of 1 m from the ground surface. In Cases 3 and 4, steel pipes were used, whereas in Case 6,
38 pipes made of flexible perforated Silicone pipes were used. In all the cases, the surface layer
39 of 0.2 m made of soil mixed with fibre was provided.

40 During the test, the foundation layer was first saturated in 1g condition, and the flood was
41 simulated by raising the water level in the supply section in 20g condition. In Cases 1, 3 and
42 4, the rising rate of the flood water was small and was in a range of 0.03-0.06 m/hr, while that
43 was large and was around 0.3 m/hr in Case 6. If the topographical conditions in Japan are taken
44 into consideration, the rising rate of flood water level 0.03-0.06 m/hr is rather slow while the
45 rising rate of 0.3m/hr is a reasonable value. This difference in the rising rate did not allow
46 direct comparison on time reference among all the cases. Experiment results showed that steel
47 drainage pipes through the drainage function limited rise of the phreatic surface, and the rigid
48 pipe provided additional reinforcement against flooding. From the experiment, while the
49 working mechanism of steel drainage was confirmed, the comparative performance of steel

50 drainage pipe with its counterpart having only one of the functions of drainage or reinforcement
51 could not be confirmed explicitly.

52 **2 Numerical analysis method validation**

53 **2.1 Constitutive models used**

54 Three-dimensional finite element analysis is conducted using the finite element code developed
55 by the last author. First validation is made by comparative studies of the numerical analysis
56 and centrifuge experiment results having different flooding patterns. Equations solved in the
57 numerical analysis are described here.

58 The equilibrium equation for soil is expressed as

$$59 \quad \frac{\partial \sigma_{ji}}{\partial x_j} + \bar{\rho} b_i = 0 \quad (1)$$

60 where density with soil, water and air mixture $\bar{\rho}$ is given by

$$61 \quad \bar{\rho} \equiv n S_r \rho_w + (1 - n) \rho_s \quad (2)$$

62 Here, σ_{ij} = total stress, ρ_w = density of water, ρ_s = soil particle density, n = porosity, S_r = degree
63 of saturation.

64 Governing equation for pore water is expressed as

$$65 \quad S_r \dot{\epsilon}_{jj} + C \dot{h}_p + \frac{\partial}{\partial x_i} \left(-k_{wu} \frac{\partial h}{\partial x_i} \right) = 0 \quad (3)$$

66 In Equation (3), C is referred to as specific moisture capacity from the soil-water characteristic
67 curve (corresponds to the slope of the relationship between pressure head with volumetric water
68 content). In the equation, h and h_p represent the total head and pressure head ($= \frac{u_w}{\rho_w g}$),
69 respectively. Pore air pressure (u_a) is assumed to be equal to atmospheric pressure which is a
70 reasonable assumption as the monotonic rise of a phreatic surface due to flooding is considered

71 in this study. k_{wu} is unsaturated hydraulic conductivity. Unsaturated hydraulic conductivity is
 72 calculated from specific permeability k_{wr} (ratio of unsaturated hydraulic conductivity k_{wu} to
 73 saturated hydraulic conductivity, k_{ws}) and the model proposed by Kosugi (1999) is used;

$$74 \quad k_{wr} = S_e^{0.5} \left\{ 1 - \left(1 - S_e^{1/m} \right)^m \right\}^2 \quad (4)$$

75 where S_e = effective degree of saturation. In the computation, the soil is modelled as an
 76 elastoplastic material and the Drucker-Prager model (Drucker and Prager, 1952) is used for the
 77 yield surface and the effective stress σ'_{ij} is expressed using equation proposed by Bishop
 78 (1960);

$$79 \quad \sigma'_{ij} = (\sigma_{ij} - u_a) + \chi(u_a - u_w) \quad (5)$$

80 with $\chi = S_e$. van Genuchten model (van Genuchten, 1980) is used for modelling the soil-water
 81 characteristic curve (SWCC) of the unsaturated soil. Using the van Genuchten closed-form
 82 equation, S_e is calculated as the function of the suction.

83 **2.2 Numerical analysis conditions**

84 **2.2.1 Modelling of the river levee**

85 River levees in the analysis are modelled as in the centrifuge experiment. The properties of
 86 the soil used in numerical analysis are presented in **Table 2**. The foundation bottom is
 87 modelled as an impermeable layer and fixed rigid connection (displacement is constrained to
 88 zero). The sides of the foundation on the protected side are modelled as impervious surfaces.
 89 As for the displacement constraint, vertical side boundaries are constrained in the horizontal
 90 direction. All the other boundary is considered permeable and there is no constraint in
 91 displacement. The boundary condition and the geometry with mesh used in the analysis are
 92 summarised in **Fig. 2**. Eight node brick elements are used in modelling both solid and liquid
 93 phases. For the solid phase, the B-bar method is employed to avoid volumetric locking. The

94 uniform size of the mesh is used in the analysis as far as possible. In the mesh, the number of
95 nodes and elements are 3393 and 2688 respectively.

96 **2.2.2 Modelling of pipes**

97 The proposed steel drainage pipe is 6 meters long, with two different sections. These two
98 sections are; 1m long section having the spiral ring made of 1 cm thick metal plate having a
99 pitch of 16 cm at the end and a 5-meter long section without spiral rings. For the numerical
100 analysis, the spiral ring is not considered and only the embedment length of the pipe in the
101 centrifuge experiment which is 5.6 m is considered and placed at a horizontal spacing of 1 m
102 and an elevation of 1 m from the ground surface. The dimension and properties of the steel
103 drainage pipe used in the analysis are listed in **Table 3**. The drainage function is modelled as
104 the line of the nodes with a pressure head ceiling at the elevation of the nodes indicating the
105 free flow inside the pipes. The reinforcement function in the slope is modelled by adding the
106 series of elastic beam elements at the location of the pipe. Nodes for the beam element are
107 common to the nodes of the elements that model soil. So no slip between the pipe and soil is
108 considered. The relative movement is considered by the shear deformation of adjacent soil
109 elements. Pipes with only either of the functions are also modelled using drainage or
110 reinforcement function only.

111 **2.2.3 Flood simulation**

112 Flooding conditions are kept similar to the experiment condition. Each analysis is divided into
113 two phases. In the first step, a steady state before flooding is achieved by assigning the water
114 level at the foundation ground surface. This result is used as the initial condition for the second
115 step. The flooding is simulated in the second step of the analysis, which is a transient analysis.
116 In this step, the flood is simulated by increasing the water level on the right side of the model.
117 **Figure 3** shows the time histories of the supply flood water head for the centrifuge experiment.
118 In the numerical analysis for validation, the flooding is modelled as a step-wise change of the

119 flood water head in the experiment. Each step is kept five hours long and in each step, the
120 flood head is kept constant. The flood head at each step is kept the same as in the centrifuge
121 experiment at the end of each period. **Figure 3** also shows the flood used for the numerical
122 analysis later with the same flooding condition.

123 **2.3 Numerical analysis result comparison with centrifuge result**

124 Before making the comparisons under the same flooding condition, the numerical analysis
125 method is validated with the comparison with the centrifuge results. The flood water head used
126 in the centrifuge experiment (not Num_Flood in **Fig. 3**) is applied in this series of analyses.
127 **Figure 4** shows the comparisons of the time histories of pore water pressure recorded at
128 Locations A and B (see **Fig. 1**) in the experiment and numerical analysis for Cases 1, 3, 4 and
129 6. In the figure, it can be observed that the trend of rising and falling of pore water pressure
130 with increase and decrease flood head is captured by the numerical analysis. The parameters
131 here are adjusted such that the temporal change is matched in the numerical analysis. The
132 magnitude is not exactly the same as the experiment result; however, from the results, it can be
133 observed that the effect of drainage and the consequent change in pore water pressure is
134 simulated by numerical analysis.

135 **Figure 5** shows the comparisons of the axial force observed near the slope (0.4m away from
136 slope surface) in the experiment and numerical analysis along with the flood head used in
137 numerical analysis in Cases 3 and 4, respectively. Axial force here in both experiment and
138 numerical analysis is shown by considering the axial force at the start of the seepage flow as
139 zero. Thus, the axial force can be negative during an increase and decrease of the tensile force.
140 The axial force simulated in both cases is similar in the trend and magnitude. The change in
141 the axial force with the seepage flow is well captured by numerical analysis in both cases when
142 drainage is present (Case 3) and when drainage is not present (Case 4).

143 **Figure 6** shows the comparison of the time histories of settlement at Location F for Cases 1
144 and 6. From the figure, it can be observed that the trend of the increase of settlement and also
145 the point of initiation of failure indicated by the sharp change in the value of the settlement is
146 well captured by the numerical analysis. Since the experiment allowed the installation of a
147 limited number of sensors, the comparison is made with the settlement of the slope only. The
148 displacement is not very comparable, but the timing of the slope failure is predicted which is
149 relevant in a comparative study of protection in a levee. In Cases 3 and 4, as minor local
150 erosion was observed in the experiment and this cannot be modelled in the present numerical
151 analysis, no comparison of displacement is shown for these cases. However, since the
152 calculated axial force of the pipe is comparable to the experiment as shown in **Fig. 5**, it can be
153 said that the deformation of the slope can be reasonably captured in these cases.

154 Overall, the numerical analysis method used in the study can reasonably simulate the flood-
155 induced seepage in the river levee and also the effect of the drainage and reinforcement. Hence,
156 this numerical analysis method is used in the simulation with the same flooding condition.

157 **3 Comparative study of different protection measures against** 158 **flood-induced deformation**

159 For the comparative performance of the steel drainage pipe with the protection measures having
160 only one of the functions of drainage or reinforcement, a three-dimensional finite element
161 numerical analysis is performed with the same flooding condition using the same river levee
162 model in the centrifuge experiment and numerical validation. In the analysis, four different
163 Cases A.1, A.3, A.4, and A.6 are taken into consideration. In these four cases, a different level
164 of protection is provided, which is tabulated in **Table 1**. For the flood simulation, the model
165 flood hydrograph similar to the rising rate in the centrifuge test in Case 6 (Num_Flood in **Fig.**
166 **3**) is used for all the cases in this series of analyses. The flood head in the numerical simulation

167 is increased in a stepwise manner in three steps of 2.5 hours long and kept constant at the
168 maximum level for the levee for all the cases of consideration.

169 **Figure 7** shows the time histories of the settlement at the shoulder of the slope and horizontal
170 displacement at the toe of the slope, respectively, for all the cases. It can be observed that with
171 the use of protection in the river levee, the displacement is reduced significantly. In the cases
172 where the drainage is provided (Cases A.3 and A.6) both horizontal displacement and
173 settlement are reduced significantly, highlighting the importance of the drainage function in
174 the protection. In Case A.4 (only reinforcement), the rate of displacement increase is similar
175 to Case A.1 (unreinforced) in the initial stage (0-15 hrs), while further increase in the
176 displacement is restrained after that. Maximum settlement and horizontal displacement in Case
177 A.4 are almost three times those in Case A.3 (steel drainage pipes). With the use of the only
178 drainage (Case A.6) the settlement in the model ground is minimised to the same extent as in
179 the use of the steel drainage pipe (Case A.3). This implies that the reinforcement function is
180 not fully utilised in Case A.3 in the scenario considered in the analysis. However, with the use
181 of the steel drainage pipe, reinforcement may act as the backup protection in the scenario when
182 the drainage function is deteriorated possibly by blockage of pipes. In the study of the use of
183 drainage pipes made of geosynthetic material by Ozer and Akay (2021); and Saran and
184 Viswanadham (2018), it was observed that clogging drainage pipes greatly affected the
185 performance of sand slopes. Thus composite geosynthetic pipes with the dual function of
186 drainage and reinforcement were proposed for better protection in the study by Ozer and Akay
187 (2021). The steel drainage pipes provide redundant and more reliable protection to the river
188 levee. The observation and consideration above indicate that Case A.3 (steel drainage pipe)
189 can provide the best protection among the cases.

190 **Figure 8** shows the location of the phreatic surfaces after 40 hours of seepage flow for all the
191 cases. Reasons for choosing the elapsed time of 40 hrs as a reference point are that at this point

192 the supply flood level is at maximum level, and the change in displacement in most of the cases
193 is stable. In the figure, it can be observed that with the presence of drainage, the location and
194 shape of the phreatic surface in the levee are modified. The phreatic surface is at a lower
195 position and has a concave upward shape in the cases with the drainage, whereas in the absence
196 of the drainage, the shape is concave downward and the location is high. With reference to
197 **Fig. 7**, it can be said that this limited rise in phreatic surface causes limited saturation of the
198 river levee and thus ultimately limiting deformation in cases with drainage. Also, the presence
199 of the reinforcement (Case A.4) ensures less deformation compared to Case A.1 (unreinforced)
200 even though the level of the phreatic surface is similar in both cases. Table 4 summarises the
201 performance of different cases in terms of the maximum settlement, maximum horizontal
202 displacement and cross-sectional area of the levee in the unsaturated condition after 40 hrs of
203 seepage flow. The table also indicates the percentage change of these parameters in comparison
204 to Case A.3 (case with steel drainage pipes).

205 **Figure 9** shows the axial force distribution in the pipe in Cases A.4 and A.3 (cases with only
206 reinforcement and steel drainage pipes) at the different elapsed times of seepage flow (0, 10,
207 15, 20, 30 and 40 hrs). Here, the axial force shown here is the total value including the force
208 induced by the self-weight of the soil before flooding. (As the plots in **Fig. 5** are the increment
209 from the steady-state before flooding; a direct comparison cannot be made with this figure.)

210 **Figure 10** shows the location of the phreatic surfaces at the elapsed time of 0, 10, 15, 20, 30,
211 and 40 hrs of seepage flow for Case A.4 and Case A.3, respectively. With the elapsed time the
212 phreatic surface moves above the location of the pipes in Case A.4, whereas there is not much
213 change in position in Case A.3. This movement of the phreatic surface above the pipes causes
214 larger axial force mobilisation in Case A.4. In Case A.3, since there is not much change in the
215 location of the phreatic surface, axial force mobilised remains similar even after a longer
216 duration of seepage flow. Mobilisation of large axial force in Case A.4 is responsible for

217 limiting the deformation even after the rise in phreatic surface to a higher level in the river
218 levee.

219 **4 Conclusions**

220 This study investigates the effectiveness of steel drainage pipes which combine the drainage
221 and reinforcement function against flooding on a sand levee with a 1H:1V slope in comparison
222 with the pipes having either drainage only or reinforcement function through the finite element
223 analysis validated by the simulation of the centrifuge model tests. It is observed that drainage
224 is crucial in minimising the horizontal displacement and settlement of the levee. Compared to
225 the unreinforced case, the use of only reinforcement reduces the settlement and horizontal
226 displacement in levees significantly by mobilisation of axial force, but the maximum horizontal
227 displacement is 193% larger and maximum settlement is 112% larger compared to the use of
228 steel drainage pipes. With the use of the only drainage, while the maximum settlement in the
229 model ground is minimised to a similar extent (only 2.4% larger) as in the use of the steel
230 drainage pipes, the maximum horizontal displacement is 37.2% larger compared to the use of
231 steel drainage pipes. In addition, the use of steel drainage pipe protection is more reliable as
232 protection is available in form of reinforcement even when drainage function has deteriorated.
233 Thus, the performance of a levee reinforced by steel drainage pipes against flooding is more
234 redundant and reliable compared to the traditional method of protection which provides only
235 one of the functions when subjected to the same flooding. The slope considered in this study is
236 an example of an extreme case, however, the performance of the proposed steel drainage pipes
237 is also expected to be effective to prevent or minimise the possible failure in a gentler slope.
238 While in this comparative study erosion of soil around the pipe is not taken into consideration,
239 the relative performances may be influenced when the pipes are provided with drainage and
240 erosion occurs. Ensuring that erosion of soil is limited especially near the surface would allow
241 more reliable protection against flooding with the use of steel drainage pipes.

242 **Data availability**

243 The datasets generated during and/or analysed during the current study are available from the
244 corresponding author on reasonable request.

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DOI:10.1007/s10346-009-0162-7

Table 1 Protection conditions in models

Case	Level of protection	Description of protection					
		Pipe 1		Pipe 2		Pipe 3	
		R	D	R	D	R	D
Case 1/A.1 ^c	Unreinforced	N/A	N/A	N/A	N/A	N/A	N/A
Case 3/A.3	Reinforced (2 steel drainage pipes + 1 steel pipe)	○	○	○ ^a	×/○ ^b	○	○
Case 4/A.4	Reinforced (3 steel pipes)	○	×	○ ^a	×	○	×
Case 6/A.6	Reinforced (3 drainage pipes)	×	○	×	○	×	○

Note: R = reinforcement function, here pipe made of steel; D = drainage function, here pipes is tubular with holes on the surface; ○ = present; × = not present; N/A = not available, pipes not used; a = with strain gauges to measure axial force and bending moment; b = in numerical analysis for the parametric studies; c = case identification for parametric studies

Table 2 Properties of Edosaki sand

Property	Value
Soil particle density (Mg/m ³)	2.72
Average initial water content of model ground	14.7%
Angle of shearing resistance [Degree of compaction D _c = 80%] (degrees)	29
Cohesion [D _c = 80 %] (kN/m ²)	2.5
Saturated hydraulic conductivity (m/s)	
Foundation	1.5E-6
Levee	4.5E-5
SWCC parameters for van Genuchten model	
Saturated volumetric water content θ_s	0.467
Fitting parameters n	1.674
Fitting parameters α	9.223
Fitting parameters m	0.403
Dry density of foundation (Mg/m ³)	1.72
Dry density of levee (Mg/m ³)	1.45
Modulus of Elasticity (N/m ²)	2.55E5

Table 3 Properties of Steel Drainage Pipe

Parameter	Value
Internal diameter (mm)	60
External diameter (mm)	80
Length (m)	6
Embedment length (m)	5.6
Young's Modulus, E (N/m ²)	2.10E+11
Flexural rigidity, EI (Nm ²)	2.89E+5
Poisson's ratio, ν	0.3

Table 4 Comparison of the performance of Levee for different Cases

Case	Max settlement (mm)	Max horizontal displacement (mm)	Unsaturated levee cross-section area ^a (m ²)
Case A.1	Levee failure	Levee failure	9.67 (-32.5%) ^b
Case A.3	8.2	14.8	14.33
Case A.4	17.4 (+112.2%) ^b	43.48 (+193.2%) ^b	8.27 (-42.3%) ^b
Case A.6	8.4 (+2.4%) ^b	20.3 (37.2%) ^b	14.33

Note: a = 40 m² when the water table is located at the foundation ground surface level,
b = percentage change in comparison to Case A.3

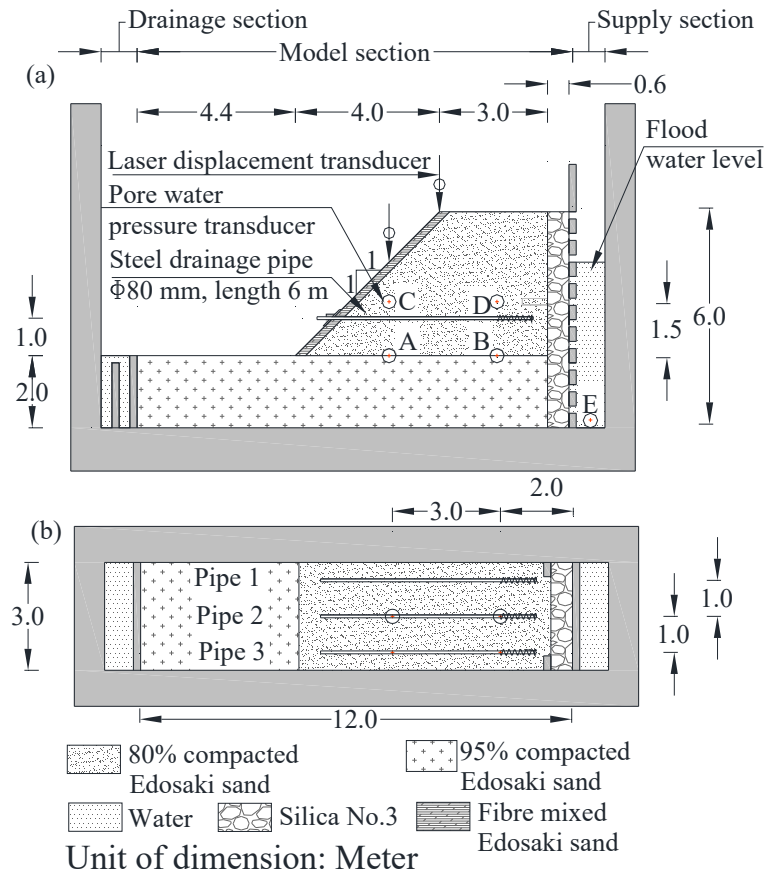


Fig 1 Model Configuration (a) sectional view with geometry and location of sensors (b) plan view (Unit of dimension: meter)

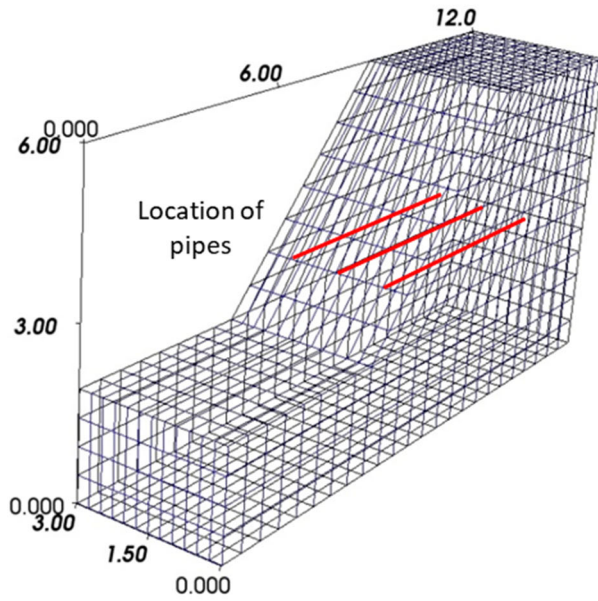
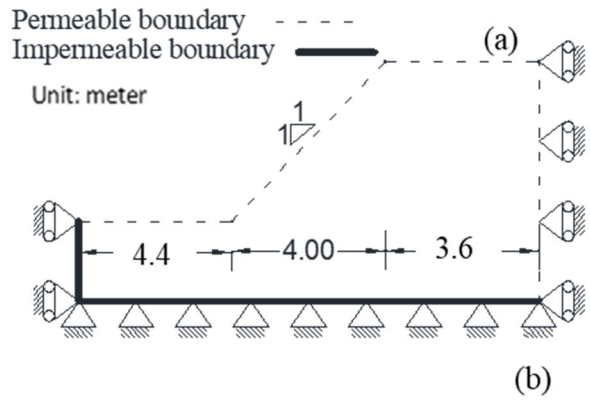


Fig 2 Finite element analysis condition (a) Boundary condition for analysis (b) Mesh for model ground

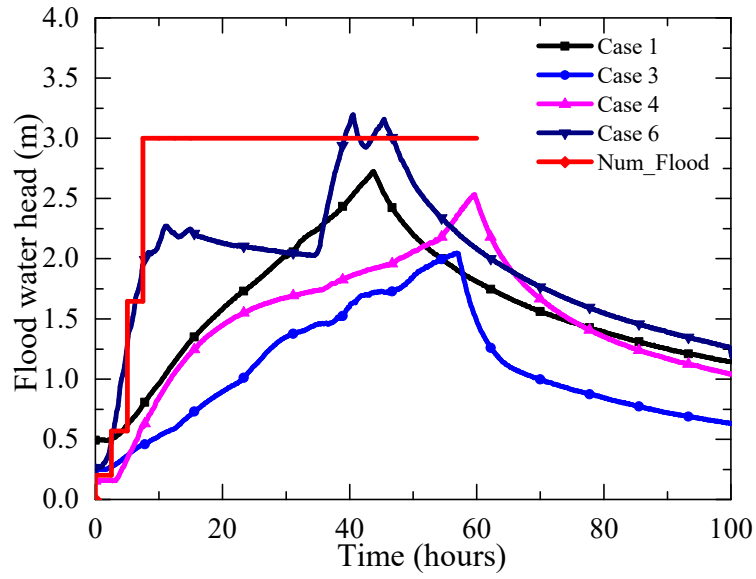


Fig 3 Time histories of supply flood water head

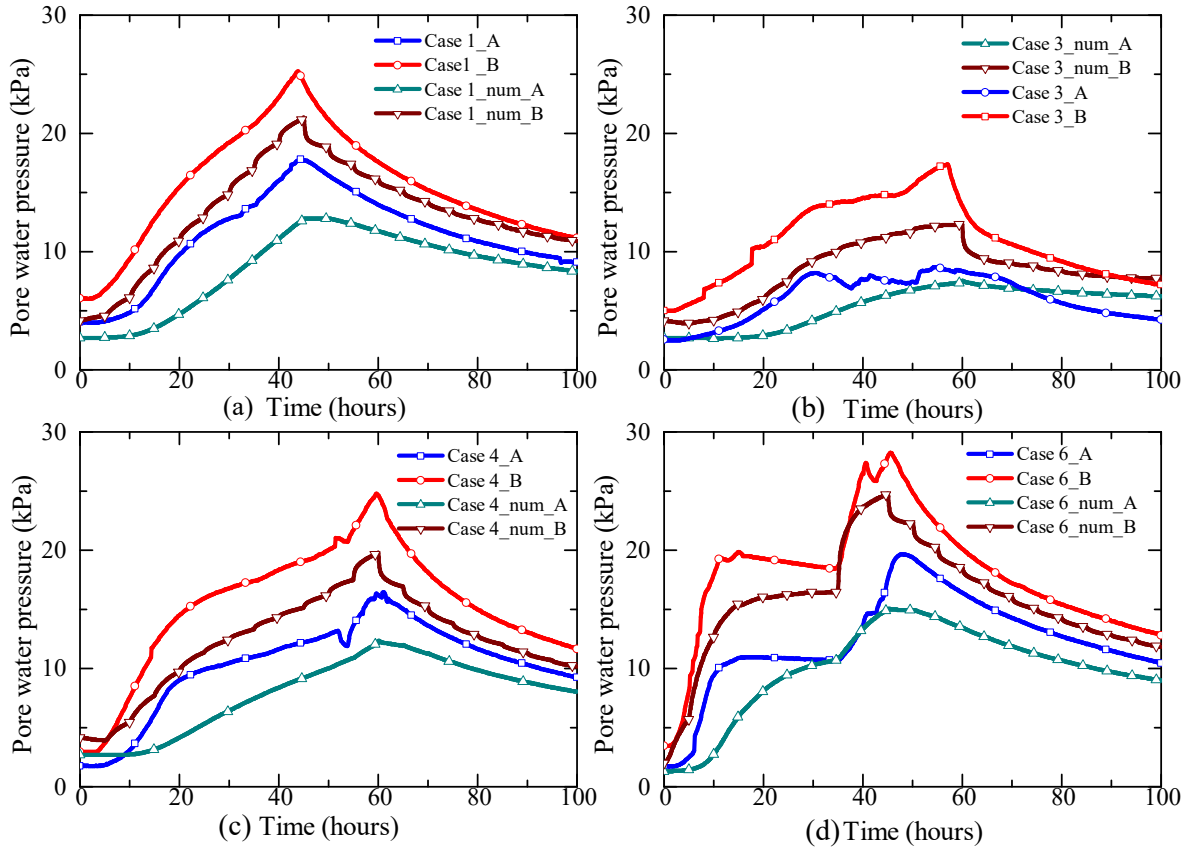


Fig 4 Comparison of the time histories of pore water pressure at locations A (below slope) and B (below crest) for (a) Case 1 (b) Case 3 (c) Case 4 (d) Case 6

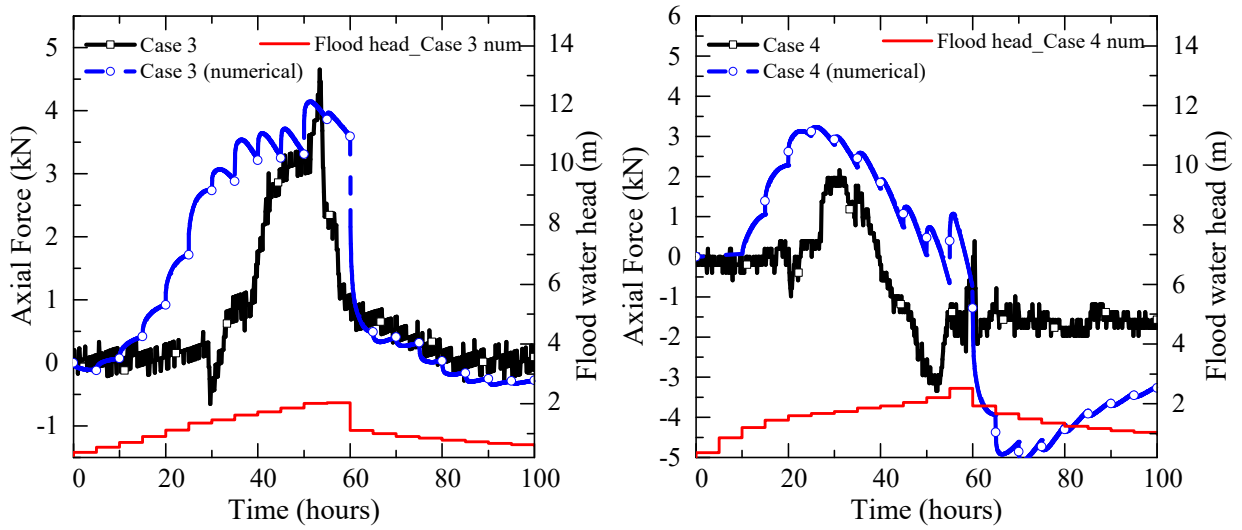


Fig 5 Comparison of the time histories of axial force at 0.4m away from slope surface (a) for Case 2 (b) for Case 3

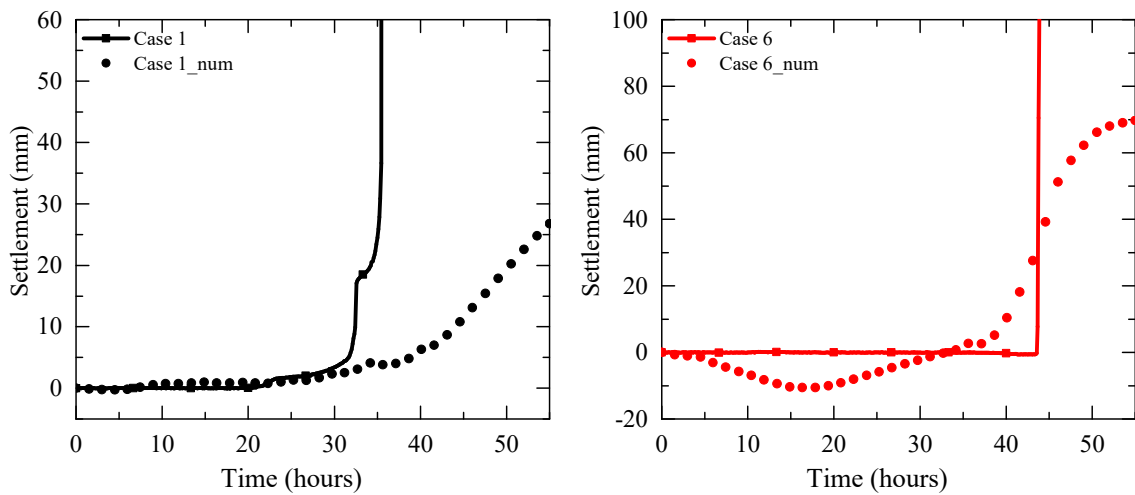


Fig 6 Comparison of the time histories of settlement at location F (a) Case 1 (b) Case 6

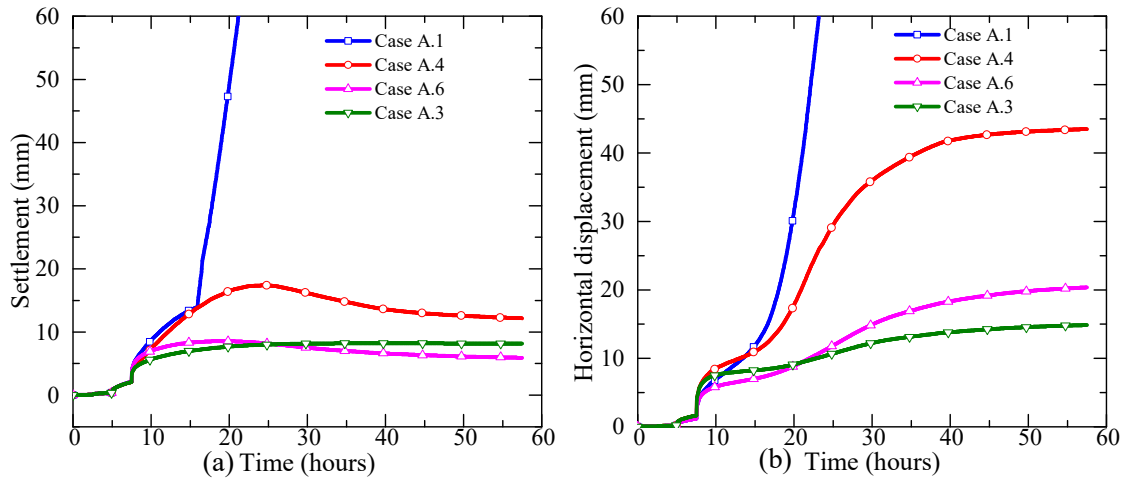


Fig 7 Time histories of displacement for all cases (a) settlement at the shoulder of slope (b) horizontal displacement at the toe of the slope

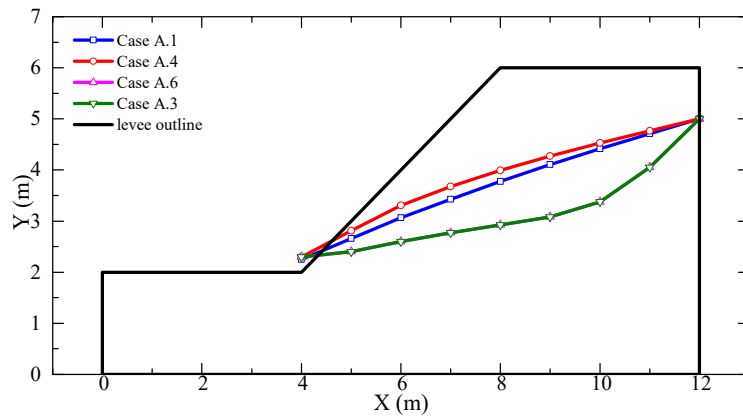


Fig 8 Location of phreatic surfaces in River levee in Cases A.1-A.4 after 40 hours of seepage flow

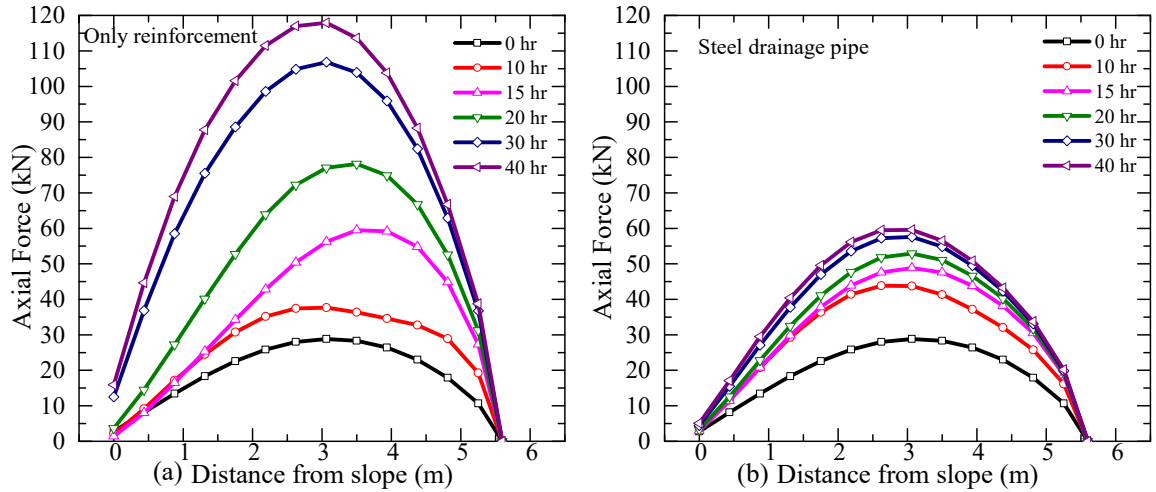


Fig 9 Axial force distribution in the pipe (a) for Case A.4 (only reinforcement) (b) for Case A.3 (steel drainage pipe)

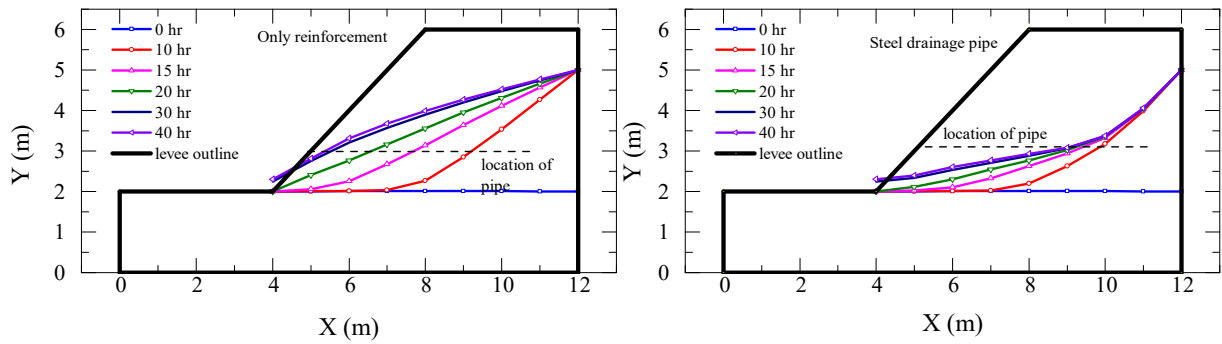


Fig 10 Location of phreatic surfaces (a) for Case A.4 (only reinforcement) (b) for Case A.3 (steel drainage pipe)