

The Past, Present, and Future of the Research on Third-Degree Price Discrimination

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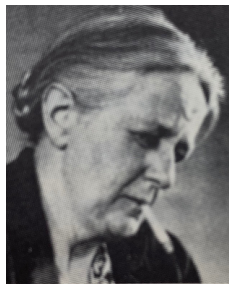
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June 27, 2021

(Revised: December 3, 2022)

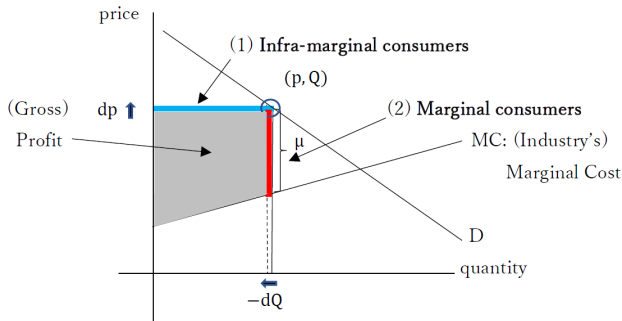
- “[I]f there is some degree of **market imperfection** there can be some degree of **price discrimination.**” (p. 180)



Joan Robinson (1903-1983)

A Price-Theoretic Perspective on Imperfect Competition

- Equilibrium Characterization (for **linear** pricing):



$$\underbrace{\theta \cdot (dp) \cdot Q}_{(1) \text{ Marginal Gain}} = \underbrace{\mu \cdot (-dQ)}_{(2) \text{ Marginal Loss}}$$

- $\theta \leq 1$: **Conduct “parameter”** ← intensity of competition
- $\mu \geq 0$: **Markup** (or Profit Margin)

“Micro-foundation” of the Conduct Parameter Approach

- There are n symmetric firms.
- Each firm j 's objective function is the sum of its own profit and the other firms' profits:

$$\hat{\pi}_j = \pi_j + \kappa \sum_{k \neq j} \pi_k,$$

where $\kappa \in [0, 1]$ measures the industry's “**attitude for cooperation**” (Shubik 1980).

- Symeonidis (2008, *JEMS*) “Downstream Competition, Bargaining, and Welfare”
 - Matsumura, Matsushima, and Cato (2013, *Econ Modelling*) “Competitiveness and R&D Competition Revisited”
 - ...
- Can allow for firm heterogeneity (κ_j).

What is Price Discrimination?

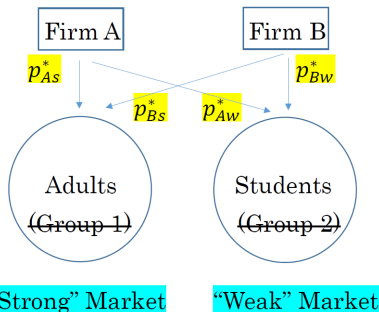
- *Price Discrimination* is “present when two or more identical units of the same products or services are sold at **different** prices, either to the same buyer or to different buyers.” (Adachi 2007, p. 392)

Taxonomy by Pigou (1920) *The Economics of Welfare*

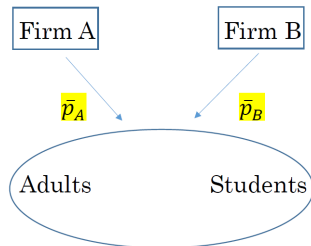
- 1st-Degree PD: Each consumer pays their WTP (willingness-to-pay).
- 2nd-Degree PD: Each consumer self-selects into a different price schedule (nonlinear pricing).
- 3rd-Degree PD: Consumers are segmented into groups by unambiguous traits (**linear** pricing).

Example: Student Discount

Price Discrimination



Uniform Pricing

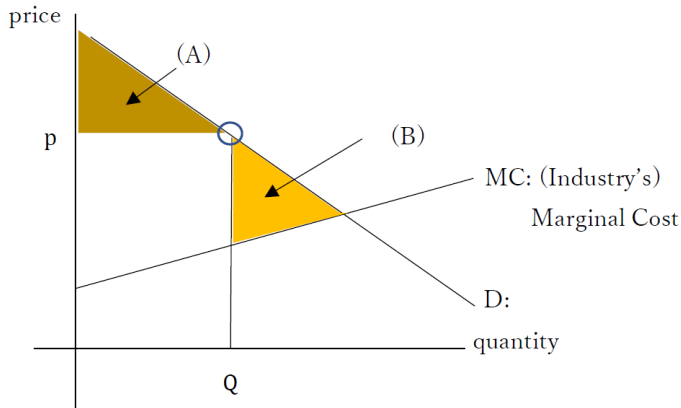


- Typically,

$$\text{Firm A: } \underbrace{p_{As}^*}_{\text{"strong" market}} > \bar{p}_A > \underbrace{p_{Aw}^*}_{\text{"weak" market}}$$

$$\text{Firm B: } \underbrace{p_{Bs}^*}_{\text{"strong" market}} > \bar{p}_B > \underbrace{p_{Bw}^*}_{\text{"weak" market}}$$

Essence of (Linear) Price Discrimination



- Cabral (2017, p.122)
 - (A): **“Exploiting surplus”** from consumers who can pay more than p (reducing consumer surplus)
 - (B): **“Generating surplus”** from consumers with potential gains from trade (reducing deadweight loss)

1. Past

A Centennial Tradition

- Generation I: Pigou (1920), Robinson (1933)

- Generation II:

Monopoly: Schmalensee ('81 *AER*), Varian ('85 *AER*), Schwartz ('90 *AER*), Nahata, Ostaszewski, and Sahoo ('90 *AER*)

Oligopoly: Holmes ('89 *AER*), Corts ('98 *RAND*)

Surveyed by Varian ('89), Armstrong ('06, '08), Stole ('07)

- More recent studies:

Monopoly: Cowan ('07; '12; '16; '18), Aguirre, Cowan, and Vickers ('10 *AER*), Chen and Schwartz ('15 *RAND*)

Oligopoly: Dastidar ('06 *Manchester*), Chen, Li, and Schwartz ('21 *RAND*), Miklós-Thal and Shaffer ('21 *IJIO*)

Sources of Inefficiency from PD

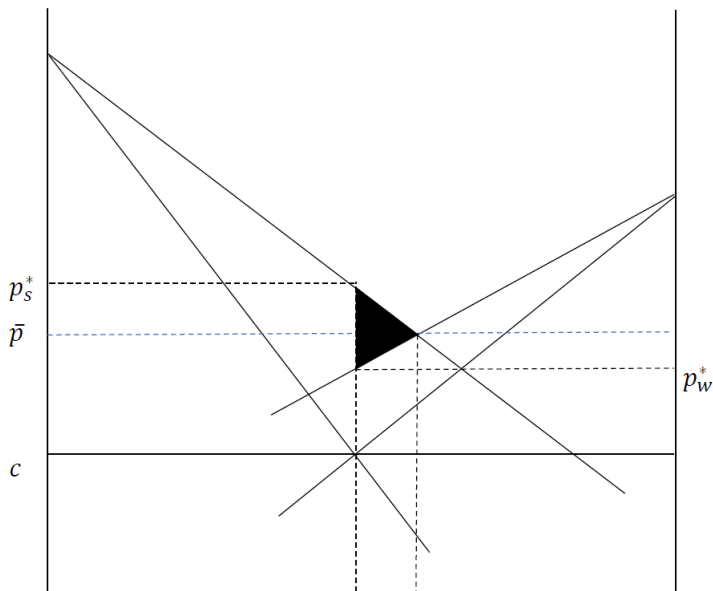
- Price Discrimination (PD):

$$\frac{p_m - c}{p_m} = \frac{1}{\varepsilon_m(p_m)},$$

where ε_m is the **price elasticity** in market $m \in \{s, w\}$.

- Aggregate output over all markets is too low because $p_m > c$.
- For a given level of aggregate output, PD typically generates **interconsumer misallocations** relative to uniform pricing.
 - Aggregate output is not efficiently distributed to the higher-value ends.

Linear Demands (adapt from Layson 1988, *AER*, Fig 1)



Welfare Implications

- In general,
Increase in aggregate output is **necessary**
for social welfare to improve.

(Varian ('85 *AER*), Schwartz ('90 *AER*), Bertolotti ('04 *JIndE*))

Introducing Consumption Externalities

- Adachi ('02 *JIndE*; '05 *Economica*):
In the presence of consumption externalities, PD can improve social welfare **even if** aggregate output doesn't change.
- What are Consumption Externalities?
 - As more people buy the good, their WTP increases or decreases.
 - "Network Effects," "Congestion," "Bandwagon or Snob Effects"
- Motivation:
One's WTP depends on the **composition** of aggregate output, which will matter to welfare.

Consumption Externalities *between* Markets

- WTP of consumer (at x_m) in market m :

$$a_m - x_m + \eta \cdot q_n^e$$

for $m, n = s, w; m \neq n, \eta \in (-1, 1)$.

- Adachi's (2002) results:
 - Aggregate output **doesn't** change.
 - Aggregate consumer surplus decreases by PD.
 - However, PD **does** improve Social Welfare iff $1/2 < \eta < 1$.

Recent Contribution

- Hashizume, Ikeda, and Nariu (2021, *Econ Bulletin*) “Price Discrimination with Network Effects: Different Welfare Results from Identical Demand Functions”
- Inverse demand function:

$$a_m - (1 + \zeta)x_m + \zeta q_m^e + \eta \cdot q_n^e,$$

derived from the representative consumer's utility

$$U = a_s x_s + a_w x_w - (1 + \zeta) \frac{x_s^2 + x_w^2}{2} + \zeta (x_s q_s^e + x_w q_w^e) + \eta (x_s q_w^e + x_w q_s^e),$$

where $\zeta > -1$ is **symmetric within**-market externality.

Recent Contribution (cont'd)

- For $\zeta \geq 1/3$, PD **never** improves Social Welfare.
- For $\zeta \in (-1, 1/3)$, PD **does** improve Social Welfare iff

$$\frac{1 + 3\zeta}{2} < \eta < 1.$$

- Adachi's (2002) case, $\zeta = 0$, is nested.

Asymmetric Within-Market Externalities

- WTP of consumer (at x_m) in market m :

$$a_m - x_m + \gamma_m \cdot q_m^e$$

for $m = s, w$, $\eta_m < 1$.

- Initial guess:

Social Welfare will improve if there are (large amounts) of **negative** consumption externality in the **strong** market & of **positive** consumption externality in the **weak** market.

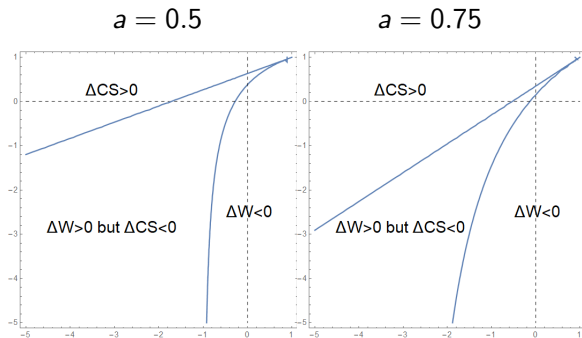
→ This is not the only case when PD improves social welfare.

Asymmetric Within-Market Externalities (cont'd)

- Adachi's (2005) results:
 - Aggregate output **doesn't** change.
 - PD **can** improve Social Welfare.
 - **Aggregate CS can increase by PD.**

Asymmetric Within-Market Externalities (cont'd)

- Wlog, $a_s = 1$ (strong) & $a_w = a \in (0, 1)$ (weak)



- For $\gamma_s > 0$ & $\gamma_w < 0$, $\Delta W < 0$.
- When $\gamma_s < 0$ & $\gamma_w < 0$, the **smaller** a , the larger is the area of $\Delta W > 0$.
- When $\gamma_s > 0$ & $\gamma_w > 0$ or $\gamma_s < 0$ & $\gamma_w > 0$, the **larger** a , the larger is the area of $\Delta W > 0$.

Asymmetric Within-Market Externalities (cont'd)

- Intuition:
 - When $\gamma_s < 0$ & $\gamma_w < 0$, the **smaller** a , the larger is the area of $\Delta W > 0$.
 - The negative size effect on $|\Delta CS_s|$ is small because $\gamma_s < 0$.
 - Small a is favorable because the effect of $\gamma_w < 0$ on ΔCS_w keeps small.
 - When $\gamma_s > 0$ & $\gamma_w > 0$ or $\gamma_s < 0$ & $\gamma_w > 0$, the **larger** a , the larger is the area of $\Delta W > 0$.
 - For $\gamma_w > 0$, when the size of the weak market is large, ΔCS_w is large enough.

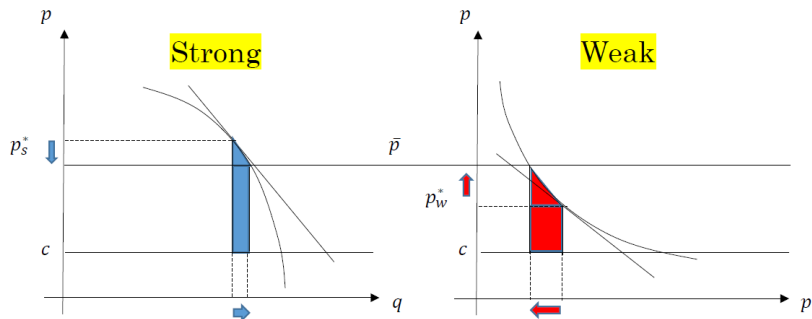
Some Other Work

- Okada and Adachi (2013, *J Ind Comp Trade*) “Third-Degree Price Discrimination, Consumption Externalities, and Market Opening”
- Adachi and Matsushima (2014, *Econ Inquiry*) “The Welfare Effects of Third-Degree Price Discrimination in a Differentiated Oligopoly”

2. Present

Aguirre, Cowan, and Vickers (2010 *AER*, Prop 2)

- “If inverse demand in the weak market is more convex than that in the strong market at the discriminatory prices, then price discrimination raises social welfare.”



- Welfare and output effects of oligopolistic third-degree price discrimination in a **fairly general setting**:
 - **General demands**
 - **Cost differences** across discriminatory markets ($c_s \neq c_w$)
 - **Firm heterogeneity**

Definition of Price Discrimination

- Here, price discrimination is defined by $p_S > p_W$ as above.
- Clerides (2004, *Econ Inquiry*, p. 402):
(**Once cost differentials are allowed,**)
“there is **no single, widely accepted definition of price discrimination.**”
- Two other alternative definitions:
 1. **Margin** definition: $p_S - c_S > p_W - c_W$
 2. **Markup** definition: $p_S/c_S > p_W/c_W$
- Our definition is almost **identical** to the two definitions when $c_S - c_W$ is small.

Methodology (1/2)

- Transform the **discrete** regime change to a **continuous** problem.
- Add the constraint $p_s - p_w \leq r$, where $r > 0$, to the firms' profit maximization problem.
- Consider $r \in [0, r^*]$, where

$p_s - p_w = r$ is the price difference

$r = 0$: **uniform pricing**

$r = r^* \equiv p_s^* - p_w^*$: **price discrimination**

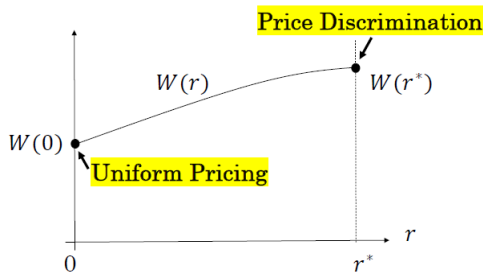
Methodology (2/2)

- Aggregate output:

$$Q(r) = 2(q_s[p_s(r)] + q_w[p_w(r)])$$

- Social welfare:

$$W(r) = U_s(q_s[p_s(r)]) + U_w(q_w[p_w(r)]) \\ - 2c_s \cdot q_s[p_s(r)] - 2c_w \cdot q_w[p_w(r)]$$



Properties of $W(r)$

- Recall social welfare is expressed as:

$$W(r) = \sum_{m=s,w} U_m(q_m[p_m(r)]) - 2 \sum_{m=s,w} c_m \cdot q_m[p_m(r)]$$

- Define

$$z_m(p) \equiv \frac{(p - c_m)q'_m(p)}{\pi''_m(p)}$$

so that $\text{sign}[W'(r)] = \text{sign}\{z_w[p_w(r)] - z_s[p_s(r)]\}$.

- Interpretation: $(p - c_m)q'_m(p)$ is the **marginal effect of a price change on social welfare** in m :

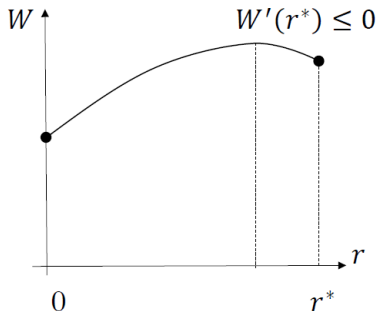
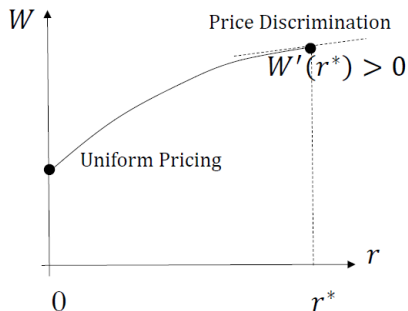
$$\frac{\overbrace{d\left[\frac{1}{2}U_m[q_m(p)] - c_m q_m(p)\right]}^{\text{per-firm (normalized)}}}{dp} = (p - c_m)q'_m(p)$$

Additional Assumption

Assumption (**Increasing Ratio Condition; IRC**)

$z_m(p)$ is increasing.

- Ensures concavity of $W(r)$
- Holds for a large class of demand functions



Sufficient Conditions for PD to Raise or Lower SW

Proposition 4

Suppose the IRC holds.

(i) If

$$\theta_w^* \mu_w^* \rho_w^* > \theta_s^* \mu_s^* \rho_s^*$$

holds, then price discrimination raises social welfare.

(ii) If

$$\frac{\bar{\theta}_w \bar{\mu}_w \bar{\rho}_w}{\bar{\theta}_s \bar{\mu}_s \bar{\rho}_s} \leq \frac{\pi''_w(\bar{p})}{\pi''_s(\bar{p})}$$

holds, then price discrimination lowers social welfare.

Relation to the Sufficient Statistics Approach

- “Sufficient statistics” (Chetty 2009) are:
 - (i) Conduct parameter, θ_m
 - (ii) Markup, μ_m
 - (iii) Pass-through, ρ_m
 - (iv) π''_m

(i) Conduct Parameter: Intensity of Competition

- **Conduct Parameter** in market m is defined by:

$$\theta_m(p) \equiv 1 - A_m(p),$$

where $A_m(p)$ is the **aggregate diversion ratio** in market m , defined by:

$$A_m(p) \equiv - \frac{\sum_k \partial q_{km}(p, p) / \partial p_A}{\partial q_{Am}(p, p) / \partial p_A} = (n - 1) \frac{\varepsilon_m^{\text{cross}}(p)}{\varepsilon_m^{\text{own}}(p)}$$

- Instead, easier to interpret: $\theta_m(p) = \frac{\varepsilon_m^I(p)}{\varepsilon_m^{\text{own}}(p)}$, where $\varepsilon_m^I(p) \equiv - \frac{pq'_m(p)}{q_m(p)}$ is the **industry-level** price elasticity.

\Rightarrow If $\varepsilon_m^{\text{own}} = \varepsilon_m^I$, **monopoly or full collusion** ($\theta_m = 1$).
If $\varepsilon_m^{\text{own}} \rightarrow \infty$, **perfect competition** ($\theta_m = 0$).

(ii) Markup

- **Markup** in market m is simply $\mu_m(p_m) \equiv p_m - c_m \geq 0$

(iii) Pass-through

- **Pass-through** in market m :

$$\rho_m \equiv \frac{\partial p_m}{\partial c_m} \geq 0$$

- For $r = r^*$ (full price discrimination),

$$\rho_m^* = \frac{\partial x_{Am} / \partial p_A}{\pi_m''} = \frac{1}{2 - (\sigma_m^I)^*},$$

where $\sigma_m^I(q) \equiv -qp''/p'$ is the **curvature of the inverse demand**.

- For $r < r^*$,

$$\rho_m[p_m(r)] = \frac{\partial x_{Am} / \partial p_A}{\pi_s'' + \pi_w''}.$$

Quantity Pass-through

- With constant marginal costs, **quantity pass-through** in market m under price discrimination is given by

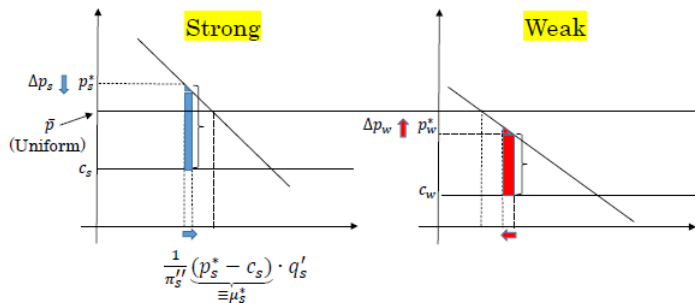
$$\begin{aligned}\frac{dq_m^*}{d\tilde{q}} &= q'_m(p_m^*) \cdot \frac{dp_m^*}{d\tilde{q}} = \frac{q'_m}{\frac{\partial x_{Am}}{\partial p_A}} \cdot \frac{\partial x_{Am}}{\partial p_A} \cdot \frac{dp_m^*}{d\tilde{q}} \\ &= \left(\frac{q'_m}{\frac{\partial x_{Am}}{\partial p_A}} \right) \cdot \left(\frac{\frac{\partial x_{Am}}{\partial p_A}}{\pi''_m} \right) = \theta_m^* \cdot \rho_m^*,\end{aligned}$$

where \tilde{q} is an exogenous amount of output with

$$\pi_{jm}(p_{jm}, p_{-j,m}) = (p_{jm} - c_m)[x_{jm}(p_{jm}, p_{-j,m}) - \tilde{q}].$$

Intuition for Part (i) of the Proposition

$$Z_m(p_m^*, c_m) = \underbrace{\mu_m^*}_{\text{Social surplus}} \times \underbrace{\theta_m^* \times \rho_m^*}_{\text{Quantity pass-through}}$$



$$\frac{1}{\pi_s'} (p_s^* - c_s) \cdot q_s'$$

$$\equiv \mu_s^*$$

$$= \mu_s^* \cdot \left(\frac{q_s'}{\pi_s'} \right) = \mu_s^* \cdot \left(\frac{q_s'}{\frac{\partial q_{As}}{\partial p_A}} \right) \cdot \left(\frac{\frac{\partial q_{As}}{\partial p_A}}{\pi_s'} \right)$$

UP lowers social welfare!

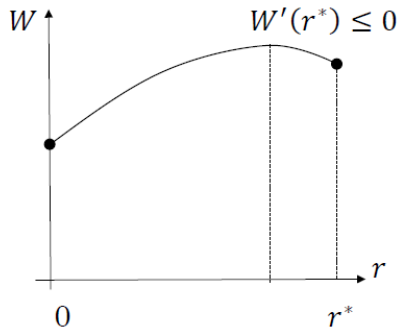
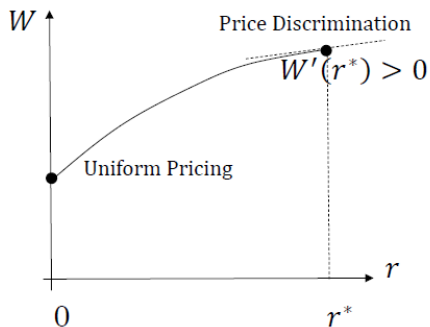
$$= \mu_s^* \cdot \theta_s^* \cdot \rho_s^* < \mu_w^* \cdot \theta_w^* \cdot \rho_w^*$$

Caveat (1)

$$W'(r^*) > 0$$



Price Discrimination Better than Uniform Pricing



Caveat (2): for Part (ii) of the Proposition

- For $r < r^*$,

$$\frac{W'(r)}{2} = \underbrace{(-\pi_s''\pi_w'')}_{<0} \left(\frac{\theta_w(r)\mu_w(r)\rho_w(r)}{\pi_w''} - \frac{\theta_s(r)\mu_s(r)\rho_s(r)}{\pi_s''} \right).$$

- Pass-through is no longer defined market-wise.
- If $|\pi_m''|$ is small, then π_m is “flat,” and thus the price shift $|\Delta p_m|$ in response to some change would be large.
- Hence, the role of π_w''/π_s'' is **to adjust measurement units** for ρ_w/ρ_s .
- For example, if $|\pi_w''|$ is very small, then the ρ_w is “over represented,” and thus it should be “penalized.”

Sufficient Conditions for Output and Welfare Changes

- When all firms are **symmetric**,

(a) Aggregate Output

If $\theta_w^* \rho_w^* > \theta_s^* \rho_s^*$, then $Q^* > \bar{Q}$.

If $\bar{\theta}_w \bar{\rho}_w < \bar{\theta}_s \bar{\rho}_s \bar{\Delta}$, then $Q^* < \bar{Q}$.

(b) Social Welfare

If $\theta_w^* \mu_w^* \rho_w^* > \theta_s^* \mu_s^* \rho_s^*$, then $W^* > \bar{W}$.

If $\bar{\theta}_w \bar{\mu}_w \bar{\rho}_w < \bar{\theta}_s \bar{\mu}_s \bar{\rho}_s \bar{\Delta}$, then $W^* < \bar{W}$.

*: Price Discrimination

–: Uniform Pricing

(c) Consumer Surplus

If $\mu_w^* \rho_w^* > \mu_s^* \rho_s^*$, then $CS^* > \bar{CS}$.

If $\bar{\mu}_w \bar{\rho}_w < \bar{\mu}_s \bar{\rho}_s \bar{\Delta}$, then $CS^* < \bar{CS}$.

Readily Carried Over to Firm Heterogeneity:

(a) Aggregate Output

If $[\theta_w^*]^T \rho_w^* > [\theta_s^*]^T \rho_s^*$, then $Q^* > \bar{Q}$.

If $[\bar{\theta}_w]^T \bar{\rho}_w < [\bar{\theta}_s]^T \bar{\rho}_s \bar{\Delta}$, then $Q^* < \bar{Q}$.

(b) Social Welfare

If $[[\theta_w^*]^T \circ [\mu_w^*]^T] \rho_w^* > [[\theta_s^*]^T \circ [\mu_s^*]^T] \rho_s^*$, then $W^* > \bar{W}$.

If $[[\bar{\theta}_w]^T \circ [\bar{\mu}_w]^T] \bar{\rho}_w < [[\bar{\theta}_s]^T \circ [\bar{\mu}_s]^T] \bar{\rho}_s \bar{\Delta}$, then $W^* < \bar{W}$.

(c) Consumer Surplus

If $[\mu_w^*]^T \rho_w^* > [\mu_s^*]^T \rho_s^*$, then $CS^* > \bar{CS}$.

If $[\bar{\mu}_w]^T \bar{\rho}_w < [\bar{\mu}_s]^T \bar{\rho}_s \bar{\Delta}$, then $CS^* < \bar{CS}$.

Introducing Non-constant Marginal Costs

- Note that our results so far do not crucially depend on the assumption of constant marginal cost.
- Caveat 1: Pass-through is now defined by

$$\rho_m \equiv \frac{\partial p_m}{\partial t_m},$$

where the first-order condition is replaced by

$$\partial_p \pi_m(p) = q_m(p) + (p - t_m - mc_m[q_m(p)]) \frac{\partial x_{A,m}}{\partial p_A}(p, p).$$

Introducing Non-constant Marginal Costs (cont'd)

- Caveat 2: $\theta_m^* \rho_m^*$ is no longer interpreted as quantity pass-through under price discrimination.
 - “Elasticity of the marginal cost” should be taken into account.

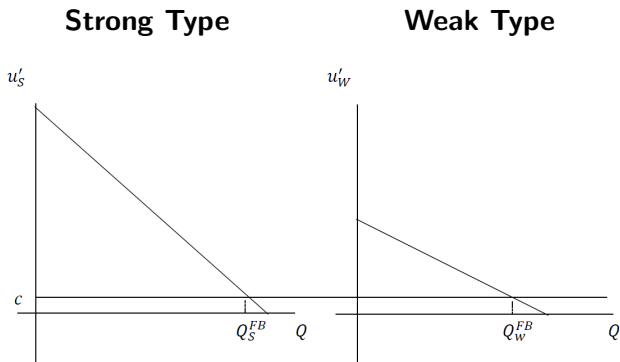
(Some) Empirical Studies

- Leslie (2004, *RAND*): Broadway theatre
- Asplund, Eriksson and Strand (2008, *JIndE*): Swedish newspaper industry
- Hendel and Nevo (2013, *AER*):
Third-degree/intertemporal price discrimination in soda sale
- Boik (2017, *Canadian J Econ*): Arbitrage
- Aryal, Murry, and Williams (2023, *REStud*): International airline markets

3. Future

Nonlinear Pricing under Imperfect Competition

- Strong type's (with mass of $\mu \in (0, 1)$) and Weak type's utility: $u_s(Q)$, $u_w(Q)$
- $u_s(Q) > u_w(Q)$ for any $Q \geq 0$
- w "nested" by s: $u'_s(Q) > u'_w(Q)$ for any $Q \geq 0$



The Case of Monopoly (Maskin and Riley 1984, *RAND*)

- Menu pricing: $\{(T_s, Q_s), (T_w, Q_w)\}$
- Strong type:

$$\begin{cases} u_s(Q_s) \geq T_s & \text{(Participation)} \\ u_s(Q_s) - T_s \geq u_s(Q_w) - T_w & \text{(Self Selection)} \end{cases}$$

$$\rightarrow T_s = u_s(Q_s) - u_s(Q_w) + T_w$$

- Weak type:

$$\begin{cases} u_w(Q_w) \geq T_w & \text{(Participation)} \\ u_w(Q_w) - T_w \geq u_w(Q_s) - T_s & \text{(Self Selection)} \end{cases}$$

$$\rightarrow T_w = u_w(Q_w)$$

(No surplus is left for the weak type)

Generalization by the Conduct Parameter Approach

$$T_w = u_w(Q_w) \quad \rightarrow \quad T_w = \theta u_w(Q_w) + (1 - \theta)cQ_w$$

- Representative firm's profit:

$$\begin{aligned} \pi = & (1 - \mu) \underbrace{\{ \theta u_w(Q_w) + (1 - \theta)c \cdot Q_w - c \cdot Q_w \}}_{\text{Tariff for the Weak type}} \\ & + \mu \underbrace{\{ u_s(Q_s) - u_s(Q_w) + \theta u_w(Q_w) + (1 - \theta)c \cdot Q_w - c \cdot Q_s \}}_{\text{Tariff for the Strong type}} \end{aligned}$$

\Rightarrow

$$\frac{\partial \pi}{\partial Q_s} = 0$$

$$\Leftrightarrow u'_s(Q_s) = c$$

A Price-Theoretic Perspective on **Nonlinear** Pricing

$$\frac{\partial \pi}{\partial Q_w} = 0$$

$$\Leftrightarrow u'_w(Q_w) = c + \underbrace{\frac{\mu}{1-\mu} \left\{ \frac{1}{\theta} u'_s(Q_w) - u'_w(Q_w) \right\}}_{\equiv K(\theta)} - \frac{\mu}{1-\mu} \frac{1-\theta}{\theta} c$$

- Then,

$$\frac{\partial K}{\partial \theta} = -\frac{\mu}{(1-\mu)\theta^2} \underbrace{\{u'_s(Q_w) - c\}}_{>0} < 0$$

→ Empirical prediction:

“As competition intensifies ($\theta \searrow$), weak type's consumption is **reduced** ($Q_w \searrow$).”

(but, not straightforward; recall the good old days like the SCP paradigm...)

- “[I]f there is some degree of **market imperfection** there can be some degree of **price discrimination.**” (p. 180)

