

# Surface Topography of Transparent Plate Using Fizeau Interferometer with Suppression of Intensity Modulation

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## Abstract

The derivation of 19-fringe phase-modulated algorithm that can suppress the first order nonlinear intensity modulation during wavelength modulating is presented. We visualize the proposed algorithm in the frequency domain in connection with the Fourier representation to discuss the properties of the algorithm. The 19-fringe algorithm yields the smallest phase error compared to the conventional algorithms. Lastly, we assess the surface of the transparent fused silica plate using the wavelength-modulating Fizeau interferometer and the 19-fringe algorithm. From the experiment results, it is indicated that the accuracy of the surface assessment for the fused silica plate is 4.0 nm.

**Keywords** Fizeau interferometer · Intensity modulation · Phase-modulated algorithm · Surface · Wavelength-modulating interferometry

## 1 Introduction

Phase-modulated interferometry has become an important technique to assess the surface and optical thickness of optical devices used in high-precision instruments in the past few decades [1,2]. By changing the phase difference between two reflected beams, three or more fringe patterns are acquired by several methods [3]. We can determine the phase distribution of the acquired patterns using a phase-modulated algorithm.

Phase modulation can occur by moving a reference mirror pushed by a piezoelectric transducer (PZT). In this case, linear miscalibration and nonlinearity of the phase modulation commonly cause systematic errors in the determined phase [1]. In addition, the phase modulation can occur by varying the wavelength of a laser diode through the variation of the injection current [4]. In phase-modulated interferometry using a laser diode, a change in laser power related to the variations of the current causes the intensity modulation of the fringe pattern that can degrade the accuracy of the interferometric

assessment [5,6].

Several authors have proposed phase-modulated algorithms to suppress the error sources [7-19]. Schwider and Hariharan proposed 5-fringe algorithm [7,8] that can suppress the linear miscalibration of the phase modulation, but not nonlinearity and intensity modulation. Larkin and Oreb derived a symmetric  $(N+1)$ -fringe algorithm [9] using a Fourier representation [20]. However, this algorithm does not suppress the intensity modulation. Surrel developed a complex polynomial theory to derive the windowed phase-modulated algorithm [12] that can suppress the linear miscalibration of phase modulation and compounding error. However, Surrel's algorithm cannot suppress the nonlinear intensity modulation.

To compensate for the bias modulation of the intensity, Onodera proposed a 6-fringe algorithm [13] based on the least-square fitting method [21]. However, it is difficult to assess the surface of highly reflective, transparent samples using Onodera's algorithm since this algorithm does not suppress the second harmonics. In case of the surface assessment of the highly reflective sample, the harmonics should be suppressed [22]. In addition, the nonlinearity of intensity modulation should be considered when applying the wavelength-modulating diode laser to actual interferometric measurements. However, there is no report regarding a phase-modulated algorithm that can suppress the nonlinear intensity modulation.

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In this paper, 19-fringe phase-modulated algorithm is derived for suppressing up to first order nonlinearity of intensity modulation. The properties of the developed algorithm are discussed by visualizing them in the frequency domain through the Fourier representation [20]. It is indicated that the phase error of the 19-fringe algorithm is the smallest compared to those of conventional phase-modulated algorithms. Finally, the surface assessment of the transparent fused silica plate is performed by combining a wavelength-modulating Fizeau interferometer with 19-fringe phase-modulated algorithm.

## 2 19-fringe Phase-modulated Algorithm

### 2.1 Complex Polynomial of Phase-modulated Algorithm

During the wavelength modulating, the signal irradiance of the fringe pattern in a laser Fizeau interferometer is defined by [22,23]

$$\begin{aligned} I(\alpha_r) &= \sum_{m=1}^{\infty} A_m \cos(\varphi_m - m\alpha_r) \\ &= I_0 \left[ 1 + \sum_{m=1}^{\infty} \gamma_m \cos(\varphi_m - m\alpha_r) \right] \end{aligned} \quad (1)$$

where  $A_m$ ,  $\varphi_m$ , and  $\gamma_m$  are the amplitude, phase, and fringe contrast of the  $m$ th harmonics and  $\alpha_r$  is a phase-modulated parameter. We can calculate the target phase  $\varphi_m$  using the phase-modulated algorithm.

When using equal intervals of  $d = 2p/N$  rad to separate the reference phases, where  $N$  is an integer, an  $M$ -fringe phase-modulated algorithm is defined by [3]

$$\varphi_m = \arctan \frac{\sum_{r=1}^M b_r I(\alpha_r)}{\sum_{r=1}^M a_r I(\alpha_r)} \quad (2)$$

where  $I(\alpha_r)$  is the  $r$ th irradiance signal defined by Eq. (1) and  $a_r$  and  $b_r$  are the  $r$ th sampling components. The design of a phase-modulated algorithm refers to the determination of sampling components  $a_r$ ,  $b_r$ , and sampling number  $M$ .

When nonlinearity occurs during wavelength modulating, the real phase-modulated value  $\alpha_r$  is a polynomial function of the ideal phase-modulated value  $\alpha_{0r}$ , including the phase-modulation error  $e$ :

$$\begin{aligned} \alpha_r &= \alpha_{0r} \left[ 1 + \varepsilon(\alpha_{0r}) \right] \\ &= \alpha_{0r} \left[ 1 + \varepsilon_0 + \varepsilon_1 \frac{\alpha_{0r}}{\pi} + \varepsilon_2 \left( \frac{\alpha_{0r}}{\pi} \right)^2 + \dots + \varepsilon_p \left( \frac{\alpha_{0r}}{\pi} \right)^p \right] \end{aligned} \quad (3)$$

where  $\alpha_{0r} = 2p[r - (M + 1)/2]/N$ ,  $e_0$  is linear miscalibration of the phase modulation,  $e_q$  ( $1 \leq q \leq p$ ) is the  $q$ th nonlinearity of phase modulation, and  $p$  is the maximum order of the nonlinearity.

For designing an error-compensating phase-modulated algorithm, many authors have proposed several systematic approaches based on the averaging method [7,11], a linear equation [10,15], and complex polynomial theory [12,14, 18,19]. Surrel developed the complex polynomial  $P(x)$  of a phase-modulated algorithm [12], defined in the following Eq. (4), to determine the phase-modulated algorithm.

$$P(x) = \sum_{r=1}^M (a_r + ib_r) x^{r-1} \quad (4)$$

where  $x = \exp(imd)$  and  $i$  is the imaginary unit.

In Surrel's theory [12], the insensitivity of the phase-modulated algorithm to the higher harmonics and phase-modulation errors is determined by the properties of the polynomial roots in the complex diagram. For instance, the phase-modulated algorithm that has single roots on the complex diagram can suppress the  $m$ th harmonics [3,12]. In addition, the phase-modulated algorithm that has a double root at  $m = -1$  is insensitive to linear miscalibration of the phase modulation  $e_0$  [9,12].

### 2.2 Derivation of 19-fringe Phase-modulated Algorithm

To compensate for linear modulation of intensity, Onodera developed a 6-fringe algorithm [13] based on the least-square fitting method [21]. Surrel described this insensitivity to the intensity modulation using complex polynomial theory [14], where

$$\sum_{r=1}^M (a_r + ib_r) r = P'(1) = 0 \quad (5)$$

From Eq. (5), insensitivity to the linear intensity modulation during wavelength modulating can be satisfied when the complex polynomial of a phase-modulated algorithm has a double root at  $m = 0$ . To compensate for the first order nonlinearity of intensity modulation, a triple root should be located at  $m = 0$  on the complex diagram of the phase-modulated algorithm. Surrel also derived a 5-fringe algorithm that has similar characteristics to those of Onodera's 6-fringe algorithm [14]. However, complex polynomials of these two algorithms do not have a root at  $m = 2$ , which means that these two algorithms are vulnerable to the second harmonics [14]. For this reason, the highly reflective surface of the silicon wafers or transparent parallel plates cannot be assessed by Onodera's 6-fringe and Surrel's 5-fringe algorithms [22,24].

In this study, Surrel's complex polynomial theory is used to derive new phase-modulated algorithms. The roots of the complex polynomial are determined considering the following requirements:

Compensation for:

- i. The  $m$ th harmonics of the signal irradiance.
- ii. The linear miscalibration and nonlinearity of the phase modulation.
- iii. The compounding errors between the higher

harmonics and linear miscalibration of phase modulation.

- iv. The first order nonlinearity of the intensity modulation while modulating the wavelength.

Satisfaction of the fringe contrast maximum condition.

To assess both surface and optical thickness of a transparent sample, we assign eight to the phase division number  $N(N=8)$  [16].

Fig. 1 represents the root location and multiplicity of the complex polynomial of the 19-fringe algorithm. First, the complex diagrams of the algorithm should contain the single roots, except at  $m = 1$  ( $x = \exp(id)$ ), to compensate for the  $m$ th harmonics [3,12]. In addition, the complex diagrams of the algorithm should contain the double roots, except at  $m = 1$ , to compensate for the linear miscalibration of phase modulation and compounding errors between the higher harmonics and linear miscalibration [12,25]. The complex diagram of the algorithm should have a triple root at  $m = -1$  to compensate for the first order nonlinear phase modulation [25]. Furthermore, the complex diagram of the algorithm should contain a triple root located at  $m = 0$  to compensate for the first order nonlinearity of the intensity modulation [25]. Finally, by locating the triple root at  $m = 2$  and 3 on the complex diagram, the fringe contrast maximum condition can be satisfied [18]. To derive the 19-fringe phase-modulated algorithm, we expand the complex polynomial shown in Fig. 1.

Based on Fig. 1, the complex polynomial  $P(x)$  of 19-fringe algorithm is given by

$$P(x) = (x-1)^3 (x-\zeta^2)^3 (x-\zeta^3)^3 \times (x+1)^2 (x-\zeta^{-1})^3 (x-\zeta^{-2})^2 (x-\zeta^{-3})^2 \quad (6)$$

where  $z = \exp(ip/4)$ . The sampling components  $a_r$  and  $b_r$  of the 19-fringe algorithm can be calculated by expanding Eq. (6) and separating the real and imaginary numbers and given to

$$a_r = \left( \begin{array}{c} 1, 2\sqrt{2} - 2, -2\sqrt{2} + 5, 0, 6\sqrt{2} - 12, \\ -16\sqrt{2} + 16, 10\sqrt{2} - 20, 0, -14\sqrt{2} + 26, \\ 28\sqrt{2} - 28, -14\sqrt{2} + 26, 0, 10\sqrt{2} - 20, \\ -16\sqrt{2} + 16, 6\sqrt{2} - 12, 0, -2\sqrt{2} + 5, 2\sqrt{2} - 2, 1 \end{array} \right) \quad (7)$$

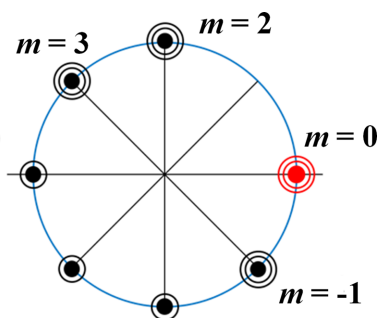


Fig. 1 Root locations of the complex polynomial for 19-fringe phase-modulated algorithm

$$b_r = \left( \begin{array}{c} -1, 0, -2\sqrt{2} + 5, 8\sqrt{2} - 8, -6\sqrt{2} + 12, \\ 0, 10\sqrt{2} - 20, -24\sqrt{2} + 24, 14\sqrt{2} - 26, 0, \\ -14\sqrt{2} + 26, 24\sqrt{2} - 24, -10\sqrt{2} + 20, 0, \\ 6\sqrt{2} - 12, -8\sqrt{2} + 8, 2\sqrt{2} - 5, 0, 1 \end{array} \right) \quad (8)$$

### 2.3 Fourier Representations of Phase-modulated Algorithms

We can visualize the phase-modulated algorithms by using Fourier representation [9,20]. To visualize the algorithms in the frequency domain, we define the sampling functions for the sampling components of the phase-modulated algorithm expressed in Eqs. (9) and (10).

$$F_1(\nu) = \sum_{r=1}^M b_r \exp(-i\alpha_r \nu) \quad (9)$$

$$F_2(\nu) = \sum_{r=1}^M a_r \exp(-i\alpha_r \nu) \quad (10)$$

where  $n$  is the frequency variable.  $F_1$  and  $F_2$  are purely imaginary and real functions based on the symmetric properties of the sampling components  $a_r$  and  $b_r$  [10,15]. Fig. 2 represents the  $iF_1$  and  $F_2$  of the 19-fringe phase-modulated algorithms.

The configuration of the sampling functions  $iF_1$  and  $F_2$  represent the error-compensating ability of the phase-modulated algorithm [9,10,14,15,18,25]. Since the sampling functions of the developed algorithm shown in Fig. 2 have zero gradients at the  $n/n_1 = 1$ , this algorithm can suppress the linear miscalibration of phase modulation and satisfy the fringe contrast maximum condition [9,18]. In addition, Fig. 2 shows that the second order derivatives of the sampling functions are zero at the  $n/n_1 = 1$ , which indicates that 19-fringe algorithm is insensitive to the first order nonlinear phase modulation. The sampling functions of the algorithm shown

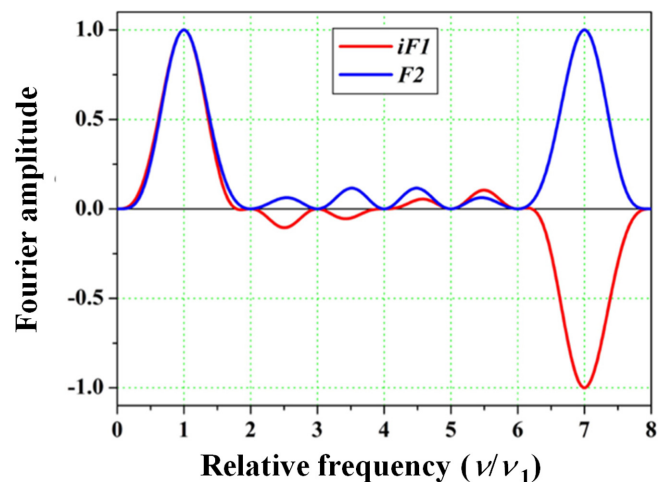


Fig. 2 Sampling functions  $iF_1$  and  $F_2$  of 19-fringe phase-modulated algorithm

above have zero gradients  $n/n_1 = 2, 3, \dots, N-2$ , which indicates a compensation ability for the compounding errors between the higher harmonics and linear miscalibration of phase modulation [15,25].

Finally, the sampling functions should have zero gradients at  $n/n_1 = 0$  to compensate for the linear modulation of intensity [14]. The sampling functions shown in Fig. 2 have zero gradients at  $n/n_1 = 0$ . In addition, the second order derivatives of the sampling functions shown in Fig. 2 are zero at the  $n/n_1 = 0$ , which indicates that 19-fringe algorithm possesses a compensation ability for the first order nonlinearity of intensity modulation.

### 3 Error Analysis

Due to the nonlinear intensity during wavelength modulating, the intensity amplitude  $A_m$  of the  $m$ th harmonics can be expressed as

$$A_m \equiv A_m (1 + \delta_0 + \delta_1 \alpha_r + \delta_2 \alpha_r^2 + \dots) \tag{11}$$

where  $d_0$  is the coefficient of intensity modulation and  $d_p$  ( $p \geq 1$ ) is the  $p$ th nonlinearity coefficient of intensity modulation. Fig. 3 shows the calculated phase error for nonlinearity of intensity defined by Eq. (11) based on the phase-modulated algorithms listed in Table 1. The phase errors shown in Fig. 3 indicate that the difference between the calculated phase without intensity modulation and the calculated phase containing nonlinear intensity using Eqs. (2) and (11).

From Fig. 3, the new 19-fringe algorithm shows the smallest calculated phase error among those of the conventional phase-modulated algorithms listed in Table 1. Particularly, by suppressing the nonlinearity of intensity  $d_1$  to a value less than 0.1, the 19-fringe algorithm achieves precise measurement with sub-nanometer accuracy. The phase errors by the Schwider-Hariharan 5-fringe [7,8] and Larkin-Oreb

**Table 1** Representative phase-modulated algorithm

Algorithm	Reference	Compensation ability	
		Error of phase modulation	Intensity modulation
New 19	-	$\varepsilon_0, \varepsilon_1$	$\delta_0, \delta_1$
Schwider-Hariharan 5	[7,8]	$\varepsilon_0$	N/A
Larkin-Oreb $N+1$ ( $N = 18$ )	[9]	$\varepsilon_0$	N/A
Hibino 11	[10]	$\varepsilon_0$	$\delta_0$
Surrel $2N-1$ ( $N = 10$ )	[12]	$\varepsilon_0$	$\delta_0$
Onodera 6	[13]	$\varepsilon_0$	$\delta_0$

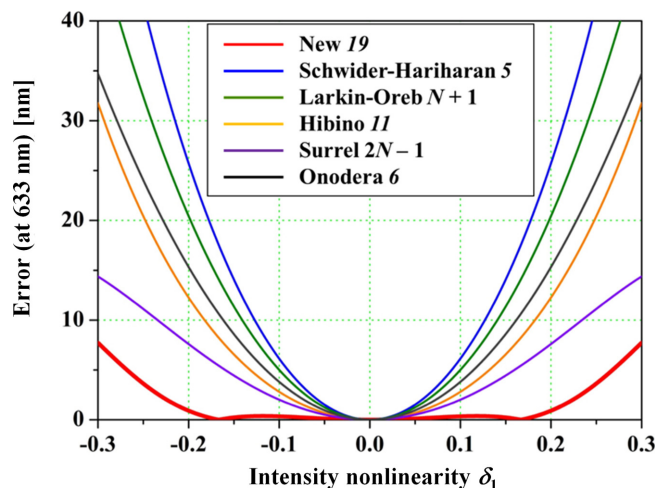
$N+1$  [9] algorithms are the largest since these algorithms do not possess the compensation ability for intensity modulation. Hibino's 11-fringe, Surrel's  $2N-1$ , and Onodera's 6-fringe algorithms can compensate for the linear modulation of intensity, but cannot compensate for the nonlinearity of intensity modulation. Therefore, these three algorithms show larger errors than that of 19-fringe algorithm.

### 4 Experiment

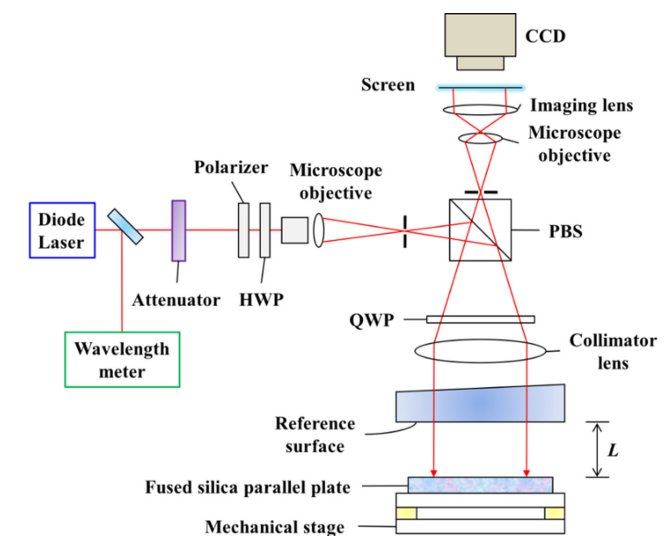
#### 4.1 Wavelength-modulating Fizeau Interferometer

By combining a wavelength-modulating Fizeau interferometer with the new 19-fringe phase-modulated algorithm, we assess the surface of an 80-mm-diameter, 8-mm-thick fused silica plate. The fused silica plate is placed horizontally on a mechanical stage with an air-gap distance of  $L = 2$  mm. Fig. 4 depicts the experimental setup for surface assessment of the fused silica plate using the wavelength-modulating Fizeau interferometer.

We maintain the laboratory temperature at 20.5°C, and use a tunable diode laser source with a Littman external cavity



**Fig. 3** Calculated phase errors of phase-modulated algorithms listed in Table 1 as functions of the nonlinearity of intensity modulation



**Fig. 4** Wavelength-modulating Fizeau interferometer for surface assessment of a fused silica parallel plate. HWP: half-wave plate; QWP: quarter-wave plate; PBS: polarization beam splitter

(New Focus TLB-6300-LN). During the surface assessment, we linearly modulate the wavelength of the diode laser source from 632.8 nm to 638.4 nm by using a picomotor and PZT [26]. The beam from the diode laser source is split by a beam splitter. Two divided beams are directed to a wavelength meter (Anritsu MF9630A) and the Fizeau interferometer. The accuracy of the wavelength meter is calibrated with  $10^{-7}$  at a wavelength of 632.8 nm. The beam incident to the interferometer illuminates the surfaces of the reference and parallel plate through the collimator lens and the reflected beams from these surfaces generate the fringe pattern. We acquire the interferogram using the CCD camera with a resolution of  $640 \times 480$  pixels.

**4.2 Results and Discussion**

Fig. 5 depicts a photo of the transparent fused silica plate in the wavelength-modulating Fizeau interferometer and a raw interferogram of the sample at a wavelength of 632.8 nm. We calculated the necessary range of wavelength modulating  $d/l$  as follows:

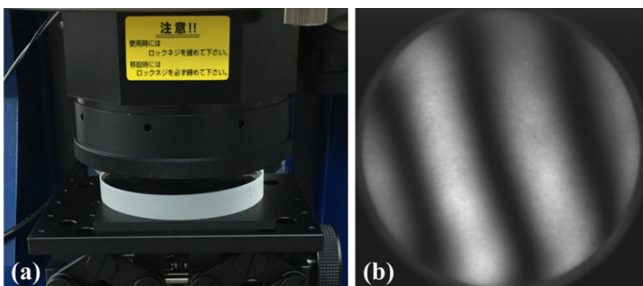
$$\delta\lambda = -\frac{\lambda^2}{4\pi L} \delta\phi \approx 0.300 \text{ nm} \tag{18}$$

We finely modulate the wavelength from 632.8198 nm to 633.1189 nm, and acquire 19 interferograms at regular wavelength intervals in 10 s. Due to the nonlinearity of the diffraction grating in the laser source, the nonlinear response of  $\sim 3\%$  occur in the PZT. For linearly modulating the wavelength of the laser source, we incrementally apply a quadratic voltage to the PZT so that the nonlinearity decrease to 1% of the total phase modulation.

We assess the surface of the fused silica plate using the acquired interferograms and proposed 19-fringe phase-modulated algorithm, as depicted in Fig. 6. The assessed surface has a concave configuration with an amplitude of  $\sim 2.2$  mm.

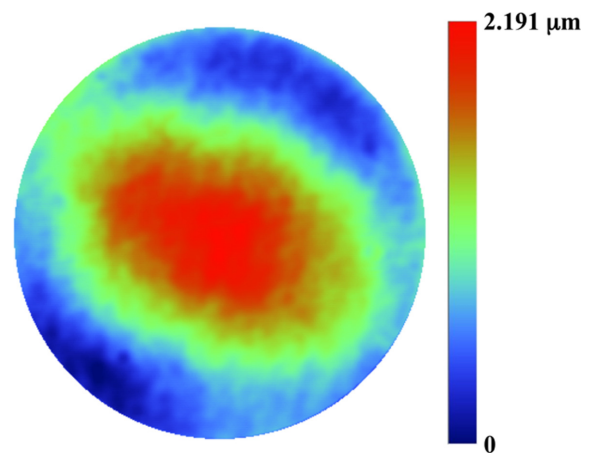
The repeatability error of the surface assessment is 4.042 nm. The uncertainty of the reference surface and the wavelength meter are  $l/20$  and  $10^{-7}$ , respectively, resulting in an overall measurement accuracy of 34 nm.

Next, the wavelength is modulated with intensity modulation, as shown in Fig. 7(a). We assess the surface of the transparent plate using the phase-modulated algorithms listed in Table 1.

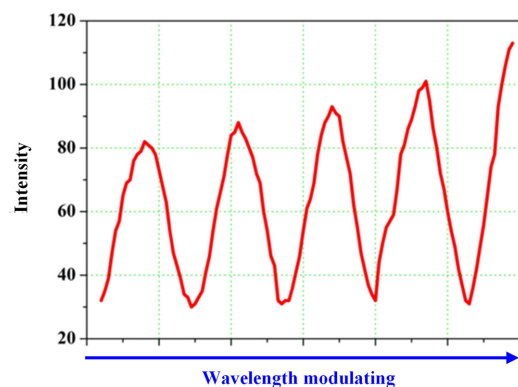


**Fig. 5** (a) Photo of fused silica plate in wavelength-modulating Fizeau interferometer and (b) Raw interferogram at a wavelength of 632.8 nm

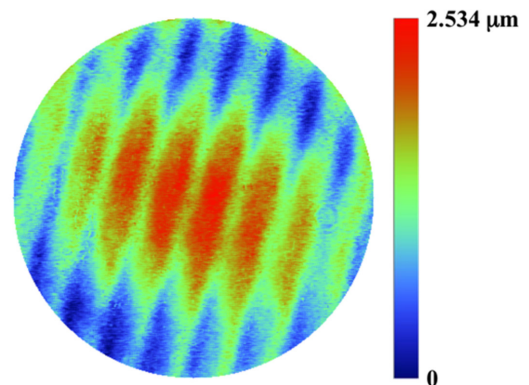
The surfaces of transparent plate assessed by these algorithms other than 19-fringe algorithm contain significant ripples due to the sensitivity to the nonlinearity of intensity modulation. As a representative of these results, Fig. 7(b) shows the surface of the transparent plate assessed by the Larkin-Oreb  $N+1$  algorithm [9]. In Fig. 7(b), considerable ripples can be observed because this algorithm does not possess the compensation ability for the intensity modulation. For intensity modulation, as shown



**Fig. 6** Surface of fused silica transparent plate assessed by 19-fringe phase-modulated algorithm



(a)



(b)

**Fig. 7** (a) Intensity modulation during wavelength modulating and (b) Measured surface of fused silica transparent plate assessed by Larkin-Oreb algorithm



in Fig. 7(a), the surface determined by the 19-fringe algorithm shows the same configuration with no ripples observed. Due to the substantial ripples, the repeatability error of the surface assessment by the Larkin–Oreb algorithm is ~885 nm.

## 5 Conclusion

We propose the derivation process for 19-fringe phase-modulated algorithm that can suppress up to first order nonlinear intensity modulation. For discussion of the properties of the phase-modulated algorithm, the developed algorithm is visualized over the frequency domain using the Fourier representation. In addition, the compensation ability for the intensity modulation is demonstrated using the phase error when nonlinearity exists during wavelength modulating. The surface assessment of the transparent fused silica plate is performed using the 19-fringe algorithm and a wavelength-modulating Fizeau interferometer. The repeatability error of surface assessment by the 19-fringe algorithm is ~4 nm. The whole measurement uncertainty is 34 nm including the accuracy of the reference surface,  $l/20\sim 30$  nm.

Even with the nonlinearity of intensity, the results calculated by the 19-fringe algorithm show almost the same configuration as for the case with no intensity nonlinearity. In contrast, the surface shapes determined using other algorithms show considerable ripples for the nonlinearity of intensity modulation.

Hence, the proposed phase-modulated algorithms are expected to enhance the managing process of the optical devices because these algorithms can suppress up to first order nonlinearity of intensity modulation when assessing the surface and optical thickness of the transparent plates. Moreover, based on Surré's complex polynomial theory, the proposed phase-modulated algorithm can be extended to suppress the higher order nonlinearity of intensity modulation.

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Fizeau interferometer and fringe analysis using phase modulating.

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